

## Study on Effects of Nonlinear Temperature Distribution and Slab Thickness on Thermal Stress of Airport Concrete Pavement

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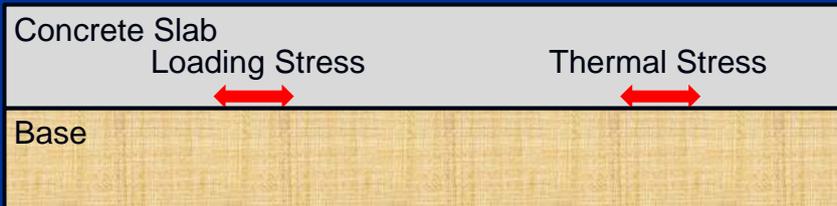
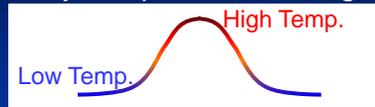
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### Background

Aircraft gear load



Daily temperature change



Design of airport concrete pavement in Japan (until 2008) is empirical design method based on U.S. PCA method.

loading stress: stress at slab center is calculated.

thermal stress: considered by Safety Factor (1.7 – 2.2).

fatigue damage:

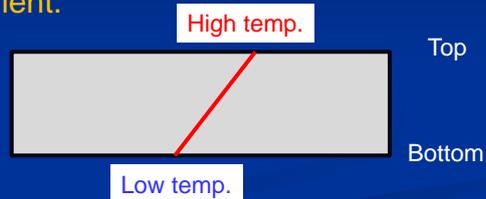
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## Background

Westergaard (1927)

Theoretical thermal (warping) stress equation for  
 linear temperature gradient.

$$\sigma = \frac{E\alpha}{2(1-\nu)}\theta$$



Thermal stress  $\sigma$  increases with temperature difference  $\theta$ .

$\sigma$ : thermal stress

$\theta$ : temperature differential between top and bottom

$E, \alpha, \nu$ : property of concrete

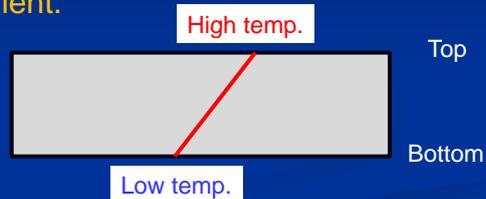
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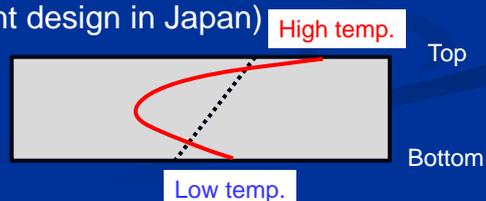
$$\sigma = \frac{E\alpha}{2(1-\nu)}\theta$$



Iwama (1964)

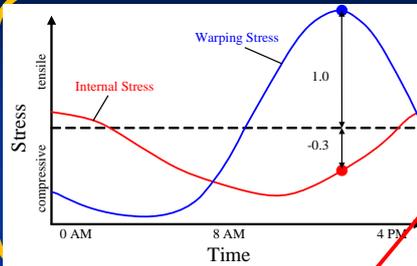
Practical thermal (warping and internal) stress equation  
 for nonlinear temperature distribution  
 (used for road pavement design in Japan)

$$\sigma = 0.7 \frac{E\alpha}{2(1-\nu)}\theta$$



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## Background



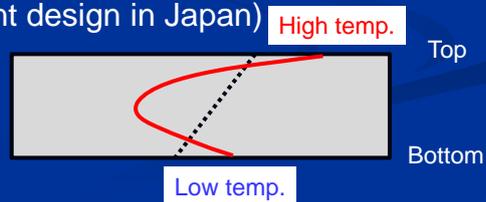
### Iwama's Observation

Internal stress tend to be **30 %** of daily maximum warping stress for 20 and 25 cm thickness

Iwama (1964)

Practical thermal (warping and internal) stress equation for **nonlinear temperature distribution** (used for road pavement design in Japan)

$$\sigma = 0.7 \frac{E\alpha}{2(1-\nu)} \theta$$



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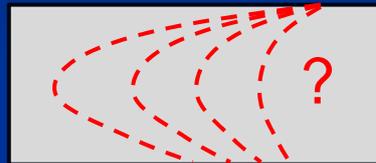
## Objective

Can the coefficient **0.7** be used for **thicker** airport pavement ?  
 Is **nonlinearity of temperature distribution** same ?



Road concrete pavement  
(20-30cm)

Coefficient = **0.7**



Airport concrete pavement  
(30-50cm)

Coefficient = ?

Practical thermal stress equation  
for thicker airport concrete pavement

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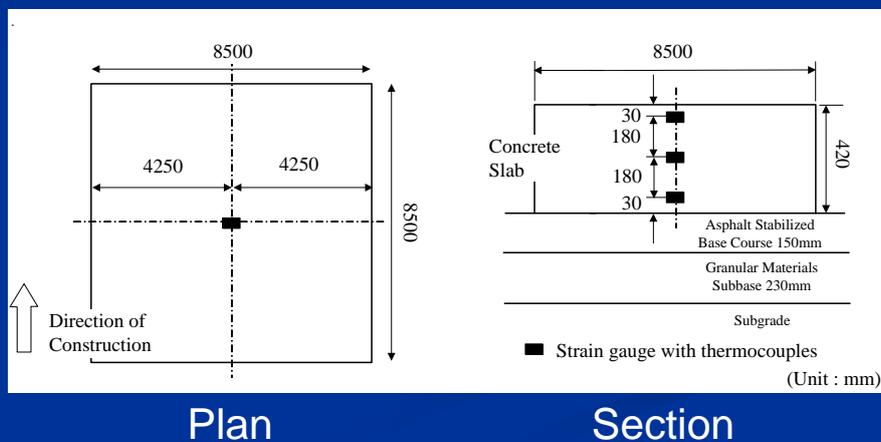
## Contents

1. Observation of 42cm thick concrete pavement  
Temperature and strain were measured for 1 year.
2. Relationship between warping stress and internal stress  
Thermal stress equation for 42cm slab thickness  
was developed.
3. Relationship between thermal stress and thickness  
By means of heat balance analysis,  
temperature distributions and thermal stress  
of various thicknesses are estimated.
4. Comparison of thicknesses

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## Observation of Experimental Pavement

Slab Size length 8.5m, width 8.5m, thickness 42cm  
Measurement strain and temperature at slab center  
every hour for one year.



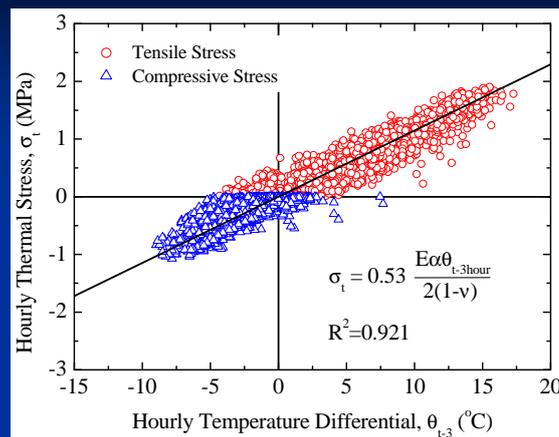
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## Thermal Stress Equation (42cm thick)



Coefficient is 0.53 for a slab 42cm thick.

The coefficient is smaller than 0.7 for 20 and 25cm

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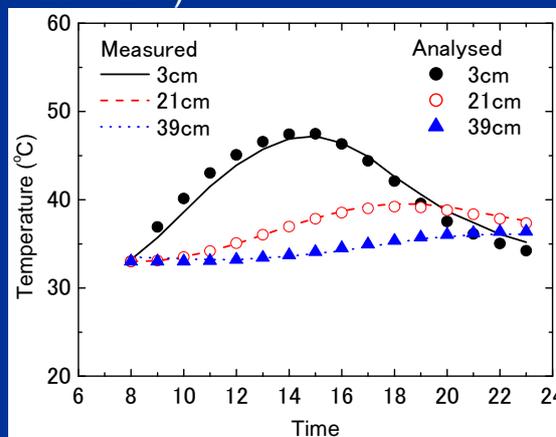
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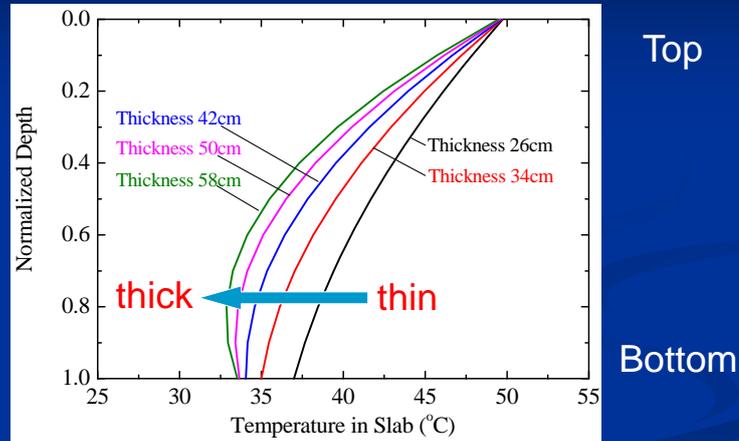
## Heat Balance Analysis

Temperature distribution in various slab thicknesses  
was estimated through **heat balance analysis**  
(heat conduction, heat transfer, solar radiation  
are considered in 2D FEM).



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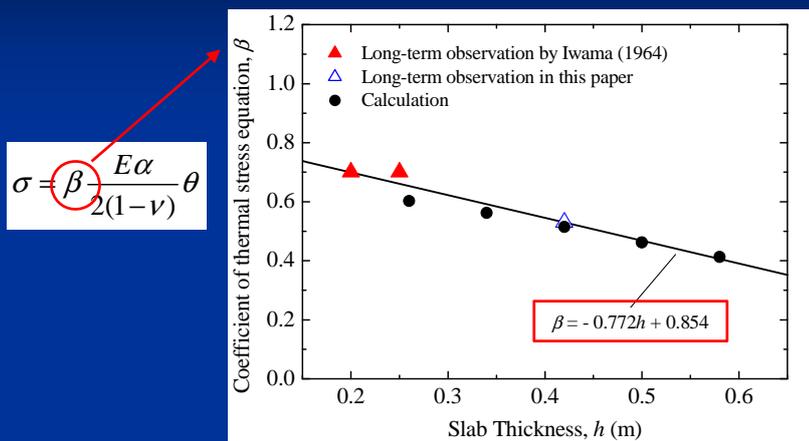
## Temperature Distribution in Various Slab Thicknesses



Nonlinearity of temperature distribution **increased** along with slab thickening.

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## Practical Thermal Equation



The coefficient tended to **decrease** with an increase in slab thickness.

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## Comparison of Thicknesses

Design of Airport Concrete Pavement in Japan was revised  
based on this research results.

Previous design method : Empirical method

Current design method : Mechanistic-Empirical method

	Design coverage (traffic volume)		
	10,000	20,000	40,000
Previous	42 cm		
Current	39 cm	41 cm	43 cm

Previous design method

Slab thicknesses are 42 cm in all cases  
because safety factors are same in 3 conditions.

Current design method

Slab thicknesses are 39 to 43 cm  
because safety factor is not used.

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## Summary and Conclusion

- (1) The coefficient of thermal stress equation **decreases** as the slab thickness **increases** because internal stress due to nonlinearity of temperature distribution across the slab is larger with increasing of slab thickness.
- (2) We propose **practical thermal stress equation for various thicknesses of slabs.**

$$\sigma = \beta \frac{E\alpha}{2(1-\nu)} \theta \quad \beta = -0.772 + 0.854h$$

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Thank you for your attention !

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